NORTH STAR
HIGH VOLTAGE

# PULSE POWER FORMULARY 

Richard J. Adler<br>North Star Research Corporation

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Contributors:
I.D. Smith, Pulse Sciences, Inc.page
R.C. Noggle, Rockwell Power Systems G.F. Kiuttu, Mission Research Corporation

Supported by<br>The Air Force Office of Scientific Research and<br>North Star Research Corporation<br>North Star High Voltage<br>12604 N New Reflection Dr<br>Marana AZ 85653<br>(520)780-9030; (206)219-4205 FAX<br>www.highvoltageprobes.com

North Star High Voltage<br>5610 Rose Loop NE<br>Bainbridge Island WA<br>(520)780-9030; (206)219-4205 FAX<br>Sales@Highvoltageprobes.com www.highvoltageprobes.com

## PVM Series Portable High

## Voltage Probes to 100 kV DC

PVM series high voltage probes are designed for general use, and for exceptional high frequency response. The probes have applications ranging from automotive ignition to excimer laser system measurement to EMI measurement. They are factory calibrated, and they do not require adjustment. In general the probes are for use with 1 Megohm oscilloscopes, but we also offer an optional switch
 which can compensate for various measurement instruments such as 10 Megohm meters as well. These units are intended for a wide range of applications where portability and ease of use are essential.

| Model Number | PVM-1 | PVM-2 | PVM-3 | PVM-4 | PVM-5 | PVM-6 | PVM-7 | PVM-11 | PVM-12 | PVM-100 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| DC/Pulsed V (kV) Max | $40 / 60$ | $40 / 60$ | $40 / 60$ | $40 / 60$ | $60 / 100$ | $60 / 100$ | $60 / 100$ | $10 / 12$ | $25 / 30$ | $100 / 150$ |
| AC RMS Voltage Max | 28 | 28 | 28 | 28 | 42 | 42 | 42 | 7 | 17 | 72 |
| Max Freq. (Mhz.) 1k:1 <br> Max Freq (Mhz) 2k:1 | 120 <br> 90 | 110 <br> 80 | 25 <br> $(10 k: 1)$ | 140 <br> 100 | 120 <br> 90 | 110 <br> 80 | 140 <br> 100 | 30 | 110 |  |
| Rise (ns) Std. Ratio | 3.0 | 3.3 | 14 | 2.5 | 3.0 | 3.3 | 2.5 | 11 | 3.3 | 3.5 |
| DC - 2 Hz. accuracy | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ | $0.15 \%$ |
| 2 Hz. - 200 Hz. <br> accuracy | $1.0 \%$ | $1.0 \%$ | $2.0 \%$ | $1.5 \%$ | $1.0 \%$ | $1.0 \%$ | $1.5 \%$ | $1.5 \%$ | $1.5 \%$ | $1.5 \%$ |
| 200 Hz.- 5 Mhz. <br> accuracy | $1.5 \%$ | $1.5 \%$ | $3 \%$ | $2 \%$ | $1.5 \%$ | $1.5 \%$ | $2 \%$ | $2 . \%$ | $2 . \%$ | $2.0 \%$ |
| 5 Mhz.-Fmax/2 <br> accuracy | $5 \%$ | $6 \%$ | $5 \%$ | $5 \%$ | $5 \%$ | $7 \%$ | $8 \%$ | $5 \%$ | $5 \%$ | $7 \%$ |
| Input R/C (Megohm/pf) | $400 / 13$ | $400 / 13$ | $400 / 10$ | $400 / 8$ | $400 / 12$ | $400 / 12$ | $400 / 8$ | $100 / 15$ | $300 / 7$ | $600 / 15$ |
| Cable Length (ft./m) | $15 / 4.5$ | $30 / 9.1$ | $100 / 30$ | $15 / 4.5$ | $15 / 4.5$ | $30 / 9.1$ | $15 / 4.5$ | $15 / 4.5$ | $15 / 4.5$ | $15 / 4.5$ |
| Cable Imp (ohm) | 50 | 50 | 50 | 50 | 50 | 50 | 50 | 50 | 50 | 50 |
| Std Ratio | 1000 | 1000 | 10,000 | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 | 2000 |
| Length (in/cm.) | $17 / 44$ | $17 / 44$ | $17 / 44$ | $17 / 44$ | $19 / 47$ | $19 / 47$ | $19 / 47$ | $7 / 18$ | $9 / 23$ | $23 / 57$ |

Add -2 to part number for 2000:1. 2000:1 may be slightly slower than 1000:1. Accuracy near the bandwidth is affected by 3 dB bandwidth considerations. The bandwidth can be " 3 db down" or " 3 db up".


5610 Rose Loop NE

Bainbridge Island, WA, 98110
(520)780-9030; (206)219-4205 FAX

Sales@Highvoltageprobes.com www.highvoltageprobes.com

## VD Series High Voltage Probes 60 to 300 kV DC

VD series high voltage probes are floor standing high voltage probes which are designed for rugged day in - day out use. They are used in a wide range of applications from radar to X-ray system quality control to advanced particle accelerator applications.
Resistors with an extremely low voltage coefficient of resistance are used, and all capacitors are temperature, frequency, and voltage stabilized for the best possible performance. The probes all have field defining toroids as a standard item in order to minimize the proximity effect (stray capacitance).
The high and low frequency calibrations are carefully matched before shipment. Very high frequency cable effects are also carefully compensated so accurate measurements can be made for short pulses. No adjustments are required after factory calibration.

| Model Number | VD-70** | VD-100 | VD-150 | VD-200 | VD-300 | VD-400 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Max DC/Pulsed V (kV) | $70 / 115$ | $100 / 160$ | $150 / 230$ | $200 / 300$ | $300 / 420$ | $400 / 550$ |
| Max Frequency (Mhz.) | 25 | 20 | 20 | 16 | 12 | 8 |
| Nom Pulse Risetime(ns) | 14 | 16 | 16 | 20 | 25 | 40 |
| Cable Length (ft.) | 30 | 30 | 30 | 30 | 30 | 30 |
| DC accuracy | $<0.1 \%$ | $<0.1 \%$ | $<0.1 \%$ | $<0.1 \%$ | $<0.2 \%$ | $<0.2 \%$ |
| 2 Hz. - 1 Mhz. Accuracy | $1 \%$ | $1 \%$ | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ |
| $>1$ Mhz Accuracy | $3 \%$ | $3 \%$ | $3 \%$ | $3 \%$ | $4 \%$ | $4 \%$ |
| Resistance (Megohms) | 1000 | 1600 | 2000 | 2800 | 2250 | 3500 |
| Height (inches/cm.) | $20 / 50$ | $24 / 60$ | $30 / 75$ | $35 / 89$ | $54 / 135$ | $72 / 180$ |
| Diameter (in/cm.) | $11 / 28$ | $11 / 28$ | $12 / 29$ | $20 / 51$ | $24 / 61$ | $24 / 61$ |
| Capacitance (approx. pf) | 23 | 25 | 27 | 24 | 30 | 30 |
| Base Diameter(in/cm.) | $10 / 25$ | $10 / 25$ | $12 / 30$ | $20 / 50$ | $30 / 76^{*}$ | $30 / 76^{*}$ |
| Standard Divider Ratio | $10,000: 1$ | $10,000: 1$ | $10,000: 1$ | $10,000: 1$ | $10,000: 1$ | $10,000: 1$ |

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## Thyratron Driver Boards



North Star High Voltage offers thyratron driver boards without chassis for general purpose use. These boards are generally combined by the user with reservoir and heater circuits to make a complete driver package. The board can then be mounted in the same enclosure with the other support circuits.
Extensive passive protection is provided for the board supported by a unique test program for the boards.

| Model Number | TT-DC/G2 | TT-G1/G2 |
| :--- | :--- | :--- |
| G2 Open Voltage <br> Pulse (kV) | 2 | 2 |
| G2 DC Bias (V) | $-150--200$ | $-150--200$ |
| G2 Short Circuit Current (A) | 30 | 20 |
| Std Rep Rate | 400 | 400 |
| Burst Rep Rate (Hz) | 600 | 600 |
| Custom Rep Rate (Hz) | $>1000$ | 1000 |
| G1 Open Voltage (V) | $150-200$ | 500 |
| G1 Short Circuit Current | 0.1 | 20 |
| BNC/Plastic Fiber Adapter | Included | Included |
| Std. Input Type | Plastic <br> Fiber | Plastic Fiber |
| Fiber adapter recommended <br> current (mA) | 20 | 20 |
| Custom Input Type | ST/SMA | ST/SMA |
| Power Input | $110 / 220$ <br> Select | $110 / 220$ Select |

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Bainbridge Island, WA
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Highvoltage@Highvoltageprobes.com www.highvoltageprobes.com

## Ignitron Drivers



Ignitrons provide a unique high current switching capability for lasers, metal forming machinery, and a variety of capacitive discharge equipment. The IG5 unit meets or exceeds all ignitron requirements. It is delivered in a die cast aluminum box with convenient mounting studs. Only line power and a trigger are required for trigger pulse production. The IG5 is provided with a DC "ready" status indicator, and a current based trigger indicator for useful feedback. We include protection networks for ringing discharge protection for all IG5-F units and the customer can use this feature or not depending on the type of discharge.

| Model Number | IG5-F | IG5-F <br> (Protected) |
| :--- | :--- | :--- |
| Open Circuit Voltage Pulse (kV) | 1.8 | 1.8 |
| Ignitor Peak Current (A, typ) | 380 | 260 |
| Closed Circuit Current (A) | 400 | 280 |
| Std Rep Rate (Hz) | 2 | 2 |
| Energy Stored (J) | 3.60 | 3.60 |
| Std. Fiber Optic Length (m) | 10 | 10 |
| Fiber adapter recommended <br> current(ma) | 20 | 20 |
| BNC/Plastic Fiber Adapter | Included | Included |
| Std. Input Type | Plastic Fiber | Plastic Fiber |
| Custom Input Type | ST/SMA | ST/SMA |
| Power Input | $110 / 220$ | $110 / 220$ |

## Table of Contents

## Contents

Introduction .....  7
1.0 FUNDAMENTAL CONSTANTS ..... 8
2.0 DIMENSIONS AND UNITS ..... 9
2.1 MKS-CGS-English Mechanical Unit Conversions ..... 10
3.0 CIRCUIT EQUATIONS ..... 11
3.1. Model Circuit Results ..... 11
3.1.1 LRC Circuit With Capacitor C1 Charged ..... 11
3.3 Capacitor Charging Circuits ..... 15
3.3.1 Resisistive Capacitor Charging, Constant Voltage Power Supply ..... 15
3.3.2 Resonant Charging ..... 16
3.4 Energies and Energy Densities ..... 16
3.5 Transformer Based Application Circuits. ..... 17
3.5.1 Transformer Equivalent Circuit ..... 17
3.5.2 Generalized Capacitor Charging ..... 18
3.6 Magnetic Switching ..... 19
4.0 TRANSMISSION LINES AND PULSE FORMING NETWORKS ..... 20
4.1 Discrete Pulse Forming Networks ..... 20
4.2 Transmission Line Pulse Generators ..... 21
5.0 ELECTRICITY AND MAGNETISM ..... 22
5.1 Transmission Line Relationships-General as Applied to Pulse Generation ..... 22
5.3 Field Enhancement Functions in Various Geometries ..... 25
6.0 MATERIALS PROPERTIES ..... 27
6.1 Solid Dielectric Properties ..... 27
6.2 Gas Properties ..... 28
6.3 Liquid Breakdown ..... 29
6.4 Vacuum Insulation and Surface Flashover. ..... 30
6.5 Conductor Properties ..... 31
6.5.1 Wire Data--Standard Sizes of Copper Wire ..... 32
6.6 Magnetic materials ..... 33
6.6.2 Resistors ..... 34
7.0 APPLICATIONS ..... 35
7.1 Intense Electron and Ion Beam Physics ..... 35
7.2 Electron Beam/Matter Interaction ..... 38
7.3 High Power Microwaves ..... 39
7.4 Railguns ..... 40
8.0 DIAGNOSTICS ..... 42
8.1 Sensitivity of an Unintegrated Square Current Loop ..... 42
8.2 Rogowski Coil ..... 42
8.3 Current Transformer ..... 43
8.4 Attenuators ..... 43
9.0 MECHANICAL DATA ..... 44
9.1 Coarse Screw Threads ..... 44
9.2 Fine Threads ..... 45
9.3 Deflection of Beams ..... 46
10.0 REFERENCES ..... 47

## Introduction

The purpose of this document is to serve the user of pulse power in the variety of tasks which he or she faces. It is intended to be used as a memory aid by the experienced pulse power engineer, and as a record of pulse power facts for those with less experience in the field, or for those who encounter pulse power only through their applications. A great deal of pulse power work involves the evaluation of distinct approaches to a problem, and a guide such as this one is intended to help speed the calculations required to choose a design approach.

In the formulary, we strived to include formulae which are 'laws of nature' such as the circuit equations, or well established conventions such as the color code. We have purposely avoided listing the properties of commercial devices or materials except where they may be regarded as generic. This has been done so that the formulary will not become obsolete too quickly. The formulas have intentionally been left in their original form, so that the use of the formulary tends to reinforce one's natural memory.

We hope to expand this document, particularly by adding new applications areas. A section on prime power systems would also be desirable. Any suggestions on formulas which have been omitted or misprinted would be appreciated.

The author would also like to thank W. Dungan and B. Smith of the US Air Force, W. Miera of Rockwell Power Systems, and J. Bayless and P. Spence of Pulse Sciences, Inc. for encouragement over the course of this and previous formula compilation efforts.

Finally, we note that few written works are without error, and that even correct information can be misinterpreted. North Star Research Corporation and the US Air Force take no responsibility for any use of the information included in this document, and advise the reader to consult the appropriate references and experts in any pulse power venture.

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## NOTE: EXPONENTS ARE PLACED IN BRACKETS AT THE END OF A NUMBER

EXAMPLE: $2.5(7)=2.5 \times 10^{7}$

### 1.0 FUNDAMENTAL CONSTANTS

Nomenclature: note that numbers in brackets are base 10 exponents
Example: $1.26 \times 10^{-6}=1.26(-6)$

| SYMBOL | NAME | VALUE-MKS(exp) | VALUE-CGS(exp) |
| :---: | :---: | :---: | :---: |
| C | Speed of light | $2.9979(8) \mathrm{m} / \mathrm{s}$ | $2.9979(10) \mathrm{cm} / \mathrm{s}$ |
| e | Electron charge | 1.6022(-19)C | 4.803(-10)esu |
| $\varepsilon_{0}$ | Free Space Permittivity | 8.8541(-12)F/m | 1 |
| $\mathrm{m}_{0}$ | Free Space Permeability | 1.2566(-6)H/m | 1 |
| h | Planck's Constant | $6.6261(-34) \mathrm{J}-\mathrm{S}$ | 6.6261(-27)erg-s |
| $\mathrm{m}_{\text {e }}$ | Electron mass | $9.1094(-31) \mathrm{kg}$ | 9.1094(-28)g |
| $m p$ | Proton mass | $1.6726(-27) \mathrm{kg}$ | 1.6726(-24)g |
| amu | Atomic mass unit | 1.6605(-27)kg | 1.6605(-24)g |
| $\mathrm{e} / \mathrm{m}_{\mathrm{e}}$ | Electron charge/mass | $1.7588(11) \mathrm{C} / \mathrm{kg}$ | $5.2728(17) \mathrm{esu} / \mathrm{g}$ |
| $\mathrm{m}_{\mathrm{p}} / \mathrm{m}_{\mathrm{e}}$ | $\mathrm{p} / \mathrm{e}$ mass ratio | 1.8362(3) |  |
| k | Boltzman constant | 1.3807(-23) J/K | 1.3807(-16)erg/K |
| N | Avogadro constant | $6.0221(23) \mathrm{mol}^{-1}$ | 1.3807(-16) rg ( |
| ${ }^{\text {s }}$ | Stefan-Boltzman constant | 5.671(-8)W $/ \mathrm{m}^{2} \mathrm{~K}^{4}$ | 5.671(-5) |
| n | Loschmidt constant | $2.6868(25) \mathrm{m}^{-3}$ | $2.6868(19) \mathrm{cm}^{-3}$ |
| atm | Standard Atmosphere | $1.0132(5) \mathrm{Pa}$ | $1.0125(6) \mathrm{erg} / \mathrm{cm}^{3}$ |
| g | Gravitational Const. | $9.8067 \mathrm{Kgm} / \mathrm{s}^{2}$ | $9.8067(5) \mathrm{gcm} / \mathrm{s}^{2}$ |

Units:

| m=meter | $\mathrm{cm}=$ centimeter | $\mathrm{s}=$ second $\quad \mathrm{q}=$ =coulomb=Amp-s |
| :--- | :--- | :--- | :--- |
| esu=electrostatic unit | F=Farad | $\mathrm{H}=$ henry $\quad \mathrm{J}=\mathrm{Joule}=\mathrm{kg}-\mathrm{m}^{2} / \mathrm{s}^{2}$ |
| $\mathrm{~kg}=$ kilogram | $\mathrm{g}=$ gram | erg=g $-\mathrm{cm}^{2} / \mathrm{s}^{2}$ |
| $\mathrm{~K}=$ degree Kelvin | $\mathrm{Pa}=$ Pascals=Kg $/ \mathrm{ms}^{2}$ |  |
| Energy Equivalence Factors |  |  |

$1 \mathrm{~kg}=5.61(29) \mathrm{MeV} \quad 1 \mathrm{amu}=931.5 \mathrm{MeV} \quad 1 \mathrm{eV}=1.602(-19) \mathrm{J}$
$\boldsymbol{\lambda}(\mathrm{m})=1.2399(-6) / \mathrm{W}(\mathrm{eV}) \quad \mathrm{W}=$ Photon Energy and $\boldsymbol{\lambda}$ is the wavelength

### 2.0 DIMENSIONS AND UNITS

In order to convert a number in MKS units into Gaussian units, multiply the MKS number by the Gaussian conversion listed. The number 3 is related to c and for accurate work is taken to be 2.9979. In this work numbers in parentheses are base 10 exponents.

| Physical Quantity | Symbol | $\begin{aligned} & \text { Dimens } \\ & \text { SI(MKS) } \end{aligned}$ | ions Gaussian | SI Units | Gaussian Conversio |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Capacitance | C | $\mathrm{t}^{2} \mathrm{q}^{2} / \mathrm{m} \mathrm{l}^{2}$ | $L$ | farad | 9(11) | cm |
| Charge | q |  | $\mathrm{m}^{1 / 2} / \mathrm{B}^{2} / \mathrm{t}$ | coulomb | 3(9) | statcoul |
| Conductivity | $\sigma$ | $\mathrm{tq}^{2} / \mathrm{m} \beta$ | 1/t | siemens/m |  | 9(9) $\mathrm{sec}^{-1}$ |
| Current | I | q/t | $\mathrm{m}^{1 / 2 / 3 / 2 /{ }^{2}}$ | ampere | 3(9) | statamps |
| Density | r | $\mathrm{m} / \beta^{3}$ | $\mathrm{m} / \beta^{\beta}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | 1(-3) | $\mathrm{gm} . / \mathrm{cm}^{3}$ |
| Displacement | D | $q / R$ | $\mathrm{m} 12 / 1 / 1 / 2 \mathrm{t}$ | coul. $/ \mathrm{m}^{2}$ | 12p(5) | stat-coul./cm ${ }^{2}$ |
| Electric field | E | $\mathrm{m} / \mathrm{t}^{2} \mathrm{q}$ | $\mathrm{m}_{12 /} / 1 / 2 \mathrm{t}$ | volt/m | (1/3)(-4) | statvolt/cm |
| Energy | U,W | $\mathrm{m} / \mathrm{t}^{2}$ | $\mathrm{mF} / \mathrm{t}^{2}$ | joule | 1(7) | erg |
| Energy density | w, e | $\mathrm{m} / \mathrm{t}^{2}$ | $\mathrm{m} / \mathrm{t}^{2}$ | joule/m ${ }^{3}$ | 10 | $\mathrm{erg} / \mathrm{cm}^{3}$ |
| Force | F | $\mathrm{m} / \mathrm{t}^{2}$ | $\mathrm{m} / \mathrm{t}^{2}$ | newton | 1(5) | dyne |
| Frequency | f | t-1 | t-1 | hertz | 1 | hertz |
| Impedance | Z | $\mathrm{m} / \mathrm{Pl}^{2}$ | t// | ohm | (1/9)(-11) | $\mathrm{sec} / \mathrm{cm}$ |
| Inductance | L | $\mathrm{m} /{ }^{2} / \mathrm{q}^{2}$ | $\mathrm{t}^{2} / /$ | henry | (1/9)(-11) | $\mathrm{sec}^{2} / \mathrm{cm}$ |
| Length | 1 | 1 | 1 | meter(m) | 1(2) | cm |
| Magnetic intens. | H | $\mathrm{q} / \mathrm{l}$ | $\mathrm{m}^{12 / 1 / 1 / 2 t}$ | amp-trn/m | $4 \mathrm{p}(-3)$ | oersted |
| Magnetic induct. | B | $\mathrm{m} / \mathrm{tq}$ | $\mathrm{m}_{1 / 2 / / 1 / 2 \mathrm{t}}$ | tesla | 1(4) | gauss |
| Magnetization | M | $\mathrm{q} / \mathrm{t}$ | $\mathrm{m}^{12 / / 4 / 2 t}$ | amp-trn/m | 1(-3) | oersted |
| Mass | m,M | m | m | kilogram | 1(3) | gram(g) |
| Momentum | p, P | $\mathrm{m} / \mathrm{t}$ | $\mathrm{m} / \mathrm{t}$ | $\mathrm{kg}-\mathrm{m} / \mathrm{sec}$ | 1(5) | $\mathrm{g}-\mathrm{cm} / \mathrm{sec}$ |
| Permeability | m | m//q2 | 1 | henry/m | 1/4p(7) |  |
| Permittivity | e | $\mathrm{t}^{2} \mathrm{q}^{2} / \mathrm{m} /{ }^{3}$ | 1 | farad/m | 36p(9) |  |
| Potential | V, F | $\mathrm{m}^{2} / \mathrm{t}^{2} \mathrm{q}$ | $\mathrm{m}^{1 / 2 / 1 / 2 / \mathrm{t}}$ | volt | (1/3)(-2) | statvolt |
| Power | P | $\mathrm{m} / 2 / \mathrm{t}^{3}$ | $\mathrm{m} / \mathrm{t}^{3}$ | watt | 1(7) | erg/sec |
| Pressure | p | $\mathrm{m} / \mathrm{t}^{2}$ | $\mathrm{m} / \mathrm{t}^{2}$ | pascal | 10 | dyne/cm ${ }^{2}$ |
| Resistivity | p | $\mathrm{m} \beta / \mathrm{tq}^{2}$ | t | ohm-m | (1/9)(-9) |  |
| Temperature | T | K | K | Kelvin | 1 | Kelvin |
| Thermal cond | k | $\mathrm{m} / \mathrm{t}^{3} \mathrm{~K}$ | $\mathrm{m} / \mathrm{t}^{3} \mathrm{~K}$ | watt/m-K | 1(5) | erg/cm-sec-K |
| Time | t | t | t | sec. | 1 | sec. |
| Vector pot. | A | $\mathrm{m} / \mathrm{tq}$ | $\mathrm{m}_{1 / 2} \mathrm{l}_{1 / 2} / \mathrm{t}$ | weber/m | 1(6) | gauss-cm |

### 2.1 MKS-CGS-English Mechanical Unit Conversions

Multiply English value by "Conversion" to obtain value in MKS units.

| Quantity | MKS(SI) | English | Conversion |
| :---: | :---: | :---: | :---: |
| Length | m | foot (ft) | $0.305 \mathrm{~m} / \mathrm{ft}$ |
| Mass | kg | Slug | $14.593 \mathrm{~kg} / \mathrm{slug}$ |
| Time | sec | Sec |  |
| Linear velocity | $\mathrm{m} / \mathrm{sec}$ | ft/sec | $0.305 \mathrm{~m} / \mathrm{ft}$ |
| Angular velocity | rad/sec | rad/sec |  |
| Linear momentum | $\mathrm{kg}-\mathrm{m} / \mathrm{sec}$ | slug-ft/sec | 0.00430 |
| Linear acceleration | $\mathrm{m} / \mathrm{sec}^{2}$ | ft ./sec ${ }^{2}$ | 0.305 |
| Angular acceleration | $\mathrm{rad} / \mathrm{sec}^{2}$ | $\mathrm{rad} / \mathrm{sec}^{2}$ |  |
| Force | Newton | pound (lb) | $4.4481 \mathrm{nt} / \mathrm{lb}$ |
| Work | $\mathrm{Nt}-\mathrm{m}$ | ft -lb | $1.356 \mathrm{Nt} / \mathrm{lb}-\mathrm{ft}$ |
| Energy | Joule | ft -lb | $1.356 \mathrm{~J} / \mathrm{ft}$ |
| Power | watt | horsepower | 747 W/hp |
| Weight | Kilogram | lb . | 0.4536 |

### 2.2 Color Code

Color Number or Tolerance (\%) Multiplier

| Black | 0 | 1 |
| :---: | :---: | :---: |
| Brown | 1 | 10 |
| Red | 2 | 100 |
| Orange | 3 | 1000 |
| Yellow | 4 | 10,000 |
| Green | 5 | 100,000 |
| Blue | 6 | 1,000,000 |
| Violet | 7 | 10,000,000 |
| Gray | 8 | 100,000,000 |
| White | 9 | 1,000,000,000 |
| Silver | 5\% | 0.01 |
| Gold | 10\% | 0.1 |
| Resistors: |  |  |
| First band = first digit; |  | Second |
| Third band = multiplier (or number of zeroes); Fourth band = toleranc |  |  |

### 3.0 CIRCUIT EQUATIONS

### 3.1. Model Circuit Results

### 3.1.1 LRC Circuit With Capacitor C1 Charged

This is the basic pulse power energy transfer stage, and so is solved in detail. An important limit is the LRC circuit with a single charged capacitor, and that circuit is the $\mathrm{C}_{2}$ goes to infinity limit of the 2 capacitor circuit.

$$
\begin{aligned}
& \mathrm{t}=\mathrm{L} / \mathrm{R} \\
& \mathrm{C}=\mathrm{C}_{1} \mathrm{C}_{2} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right) \\
& \boldsymbol{\omega}_{0}{ }^{2}=1 / \mathrm{LC} \\
& \omega^{2}=\mathrm{ABS}\left(1 / \mathrm{LC}-1 /(2 \boldsymbol{\tau})^{2}\right) \\
& \mathrm{V}_{0}=\text { initial } \mathrm{C}_{1} \text { voltage }
\end{aligned}
$$



1) Oscillatory Case
$R^{2}<4 L / C$ (underdamped)
$\mathrm{I}=\left(\mathrm{V}_{\mathrm{o}} / \boldsymbol{\omega} \mathrm{L}\right) \exp (-\mathrm{t} / 2 \boldsymbol{\tau}) \sin \omega \mathrm{t}$
$\mathrm{I}($ maximum $\left.) \simeq \mathrm{Vo}_{0} /(\mathrm{L} / \mathrm{C})^{1 / 2}+0.8 \mathrm{R}\right)$
$\mathrm{V}\left(\mathrm{C}_{2}\right)=$ 'output voltage'
$=\left[\mathrm{V}_{0} \mathrm{C}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)\right]\{1-\exp (-\mathrm{t} / 2 \boldsymbol{\tau}) \cos \boldsymbol{\omega} \mathrm{t}+(1 / 2 \boldsymbol{\omega} \boldsymbol{\tau}) \exp (-\mathrm{t} / 2 \boldsymbol{\tau}) \sin \omega \mathrm{t}\}$
$\mathrm{V}\left(\mathrm{C}_{1}\right)=\mathrm{V}_{0} \mathrm{C}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)+\mathrm{V}_{0} \mathrm{C}_{2} e(-\mathrm{t} / 2 \boldsymbol{\tau})(\cos \boldsymbol{\omega} \mathrm{t}+(1 / 2 \boldsymbol{\omega} \boldsymbol{\tau}) \sin \omega \mathrm{t}) /\left(\mathrm{C}_{1}+\right.$
$\left.\mathrm{C}_{2}\right) \mathrm{V}\left(\mathrm{C}_{2}\right.$ maximum $)=\left[\mathrm{V}_{0} \mathrm{C}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)\right]\{1+\exp (-\mathrm{p} / 2 \omega \tau)\}$
$\mathrm{V}\left(\mathrm{C}_{1}\right.$ minimum $)=\left[\mathrm{V}_{0} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)\right]\left\{\mathrm{C}_{1}-\mathrm{C}_{2} \exp (\mathrm{p} / 2 \boldsymbol{\omega} \boldsymbol{\tau})\right\}$
$Q=(L / C)^{1 / 2} / R=$ Circuit Quality Factor
2) Energy transfer to $C_{2}$ as a fraction of original $C_{1}$ energy $\boldsymbol{\eta}$
$\boldsymbol{\eta}=\left[4 \mathrm{C}_{1} \mathrm{C}_{2} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)^{2}\right]\left\{1-\exp (\mathrm{p} / 2 \boldsymbol{\omega} \boldsymbol{\tau})^{2}\right\}^{2}$

Efficiency of lossless energy transfer from $\mathrm{C}_{1}$ to $\mathrm{C}_{2}$.

## Energy Fraction


3) Overdamped case

$$
\mathrm{R}^{2}>4 \mathrm{~L} / \mathrm{C}
$$

$I=\left\{V_{o} \exp (-t / 2 \boldsymbol{\tau}) / 2 L \boldsymbol{\omega}\right\}[\exp (+\omega t)-\exp (-\omega t)]$
$\mathrm{V}\left(\mathrm{C}_{2}\right)=\left(\mathrm{V}_{0} / 2 \mathrm{C}_{2} L \boldsymbol{\omega}\right)\left\{2 \boldsymbol{\omega} / \boldsymbol{\omega}_{0}{ }^{2}-\exp (-\mathrm{t} / 2 \boldsymbol{\tau})\{\exp (\boldsymbol{\omega t} /(\boldsymbol{\omega}+(1 / 2 \boldsymbol{\tau}))\}+\{\exp (\boldsymbol{\omega t}) /((1 / 2 \boldsymbol{\tau})-\boldsymbol{\omega})\}]\right\}$
3) Shunt resistance (Underdamped) may be important in the case of water capacitors or the charge resistors in Marx generators. For the underdamped case, a resistance shunting $\mathrm{C}_{2}$ of value $\mathrm{R}_{\text {sh }}$ may be included in the output voltage equation as given below:
$\mathrm{V}\left(\mathrm{C}_{2}\right)=\left[\mathrm{V}_{\mathrm{o}} \mathrm{C}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)\right]\left\{\exp \left(-\mathrm{t} / \mathrm{R}_{\text {sh }}\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)\right)-\exp \left(-\left(\mathrm{t} / 2 \boldsymbol{\tau}+\mathrm{t} / 2 \mathrm{R}_{\text {sh }} \mathrm{C}_{2}\right)\right)[\cos \omega \mathrm{t}+(1 / 2 \omega \boldsymbol{\tau}) \sin \omega t]\right\}$

### 3.2 Marx Generators

### 3.2.1 Conventional Marx

$\mathrm{N}=$ Number of capacitor
stages
$\mathrm{C}_{2}=$ Capacitance to be charged
$L=L_{\text {switches }}+\mathrm{L}_{\text {caps }}{ }^{+} \mathrm{L}_{\text {connections }}$
$R_{s}=R_{\text {switches }}+R_{\text {caps }}$
$\boldsymbol{\tau}=\mathrm{L} / \mathrm{R}_{\mathrm{s}}$
C = Capacitance of single stage

$$
\boldsymbol{\omega}^{2}=\left(\left(\mathrm{NC}_{2}+\mathrm{C}\right) /\left(\mathrm{NLCC}_{2}\right)-1 /(2 \boldsymbol{\tau})^{2}\right)
$$

Capacitive load $=\mathrm{C}_{2}$
$\mathrm{V}\left(\mathrm{C}_{2}\right.$ max $)=\left[2 \mathrm{NV}_{0} \mathrm{C} /\left(\mathrm{C}+\mathrm{NC}_{2}\right)\right]\{1-\exp (-\boldsymbol{\pi} / \mathbf{2} \boldsymbol{\omega} \boldsymbol{\tau})\}$
Losses when charging E/ with resistance R or
 inductance $L_{c}$ per stage for $N$ stages:
$E^{\prime}=N\left(V_{0}{ }^{2} / R\right)(\boldsymbol{\pi} / \omega)$
$\mathrm{E}_{/}=\mathrm{N}\left(\mathrm{V}_{0}{ }^{2} / \mathrm{L}_{c}\right)(\boldsymbol{\pi} / \mathbf{2 \omega})^{2}$ approximately, or use the data of section 3.1 .1 where $\mathrm{C}_{1}=\mathrm{C} / \mathrm{N}$.
Resistive load $R_{L}$, where $R_{s}=R_{L}$ plus the sum of all other series circuit resistances

$$
\begin{aligned}
& \boldsymbol{\omega}^{2}=\left(\left(\mathrm{R}_{\mathrm{s}} / 2 \mathrm{~L}\right)^{2}\right. \\
& \mathrm{N} /(\mathrm{LC})) \boldsymbol{\tau}=\mathrm{L} / \mathrm{R}_{\mathrm{s}}
\end{aligned}
$$

$V_{\text {out }}=\left(N V_{0} R \exp (-t / 2 t) / 2 L \omega\right)[\exp (+\omega t)-\exp (-\omega t)]$
$\mathrm{T}_{\mathrm{m}}=(1 / 2 \boldsymbol{\omega}) \ln [(1+2 \boldsymbol{\omega} \boldsymbol{\tau}) /(1-2 \boldsymbol{\omega} \boldsymbol{\tau})]=$ time at which voltage is peak
Losses due to charging components for inductive and resistive charging during the discharge--specifically energy dissipation in the 2 N charge resistors R during the pulse, or energy left in the 2 N charge inductors $L_{c}$ at the end of the pulse:
$\mathrm{E}_{/}=\mathrm{NV}{ }_{0}{ }^{2} \mathrm{R}_{\mathrm{s}}\left(\mathrm{R}_{\mathrm{s}}{ }^{2} \mathrm{C} / 2 \mathrm{~L}-1\right) /\left(\mathrm{R}\left[\left(\mathrm{R}_{\mathrm{s}}{ }^{2} / 4 \mathrm{~L}\right)-\mathrm{N} / \mathrm{C}\right]\right)$
$E_{/}=\left(V_{0}\left(R_{L}+R\right) C\right)^{2} / N_{c}$

## Peaking circuit

Peaking circuits are used in order to get fast rise times from Marx based circuits for applications such as EMP testing. In EMP testing, an exponential waveform with a very fast rise time is required. Note that source resistances are ignored in this treatment, and that these may be included
 by referring to the treatment of 3.1.1.
$\mathrm{C}_{\mathrm{p}}=\left(\mathrm{L} / \mathrm{R}^{2}\right) /\left(1+\left(\mathrm{L} / \mathrm{R}^{2} \mathrm{C}_{1}\right)\right)$
is the peaking capacitance required to give an exactly exponential decay through the load resistance $R$. The switch is arranged to fire when the current is maximum at
$\mathrm{t}=\left(\mathrm{LC} \mathrm{CP}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{\mathrm{P}}\right)\right)^{1 / 2} \cos ^{-1}\left(\mathrm{C}_{\mathrm{P}} / \mathrm{C}_{1}\right)$

LC Marx
'Vector Inversion Type'
Open circuit voltage
$\boldsymbol{\omega}^{2}=1 / L C, \boldsymbol{\tau}=L / R$
$\mathrm{V}=(\mathrm{nV} / 2)(1-\exp (-\mathrm{t} / 2 \boldsymbol{\tau}) \cos \omega \mathrm{t})$


### 3.3 Capacitor Charging Circuits

| TYPE | Application | Advantages | Disadvantages |
| :---: | :---: | :---: | :---: |
| Resistive, No filter Capacitor | Low voltage, Small Caps. | Simple | Low eff. (50\%) |
| Inductive | Pulse charging | Efficient Doubles voltage | Requires store capacitor, 1st pulse half voltage |
| Pulse Transformer | High voltage pulse charging | Efficient | Complex, Expensive |
| Resonant Pulse | High voltage pulse charging | Efficient | Complex, Capacitors undergo reversal |
| AC resonant | Pulse charge | Efficient | Not versatile |
| Switcher | All | Efficient |  |

### 3.3.1 Resisistive Capacitor Charging, Constant Voltage Power Supply

| $\mathrm{R}=$ charge resistance <br> $\mathrm{V}_{\mathrm{o}}=$ power supply voltage <br> $\mathrm{C}=$ capacitance to be <br> charged |
| :---: |
| $\mathrm{V}(\mathrm{t})=\mathrm{V}_{0}\left(1-\mathrm{e}^{-\mathrm{t} / \mathrm{RC}}\right)$ |
| $\mathrm{I}(\mathrm{t})=\mathrm{V}_{0} \mathrm{e}^{-\mathrm{t} / \mathrm{RC}}$ |
| $\mathrm{V} / \mathrm{V}_{0}(\%)$ |
| $======================$ |
| 50 |
| 75 |
| 90 |



### 3.3.2 Resonant Charging


$l(t)=\left(V_{1} / \omega L\right)$ sin $\omega t$, where
$\mathrm{V}_{2}(\mathrm{t})=\mathrm{V}_{1}\left(\mathrm{C}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)\right)(1-\cos \omega \mathrm{t})$
$\mathrm{V}_{2} \max =\mathrm{GV}$, where ringing gain, $\mathrm{G}=2 \mathrm{C}_{1} /\left(\mathrm{C}_{1}+\mathrm{C}_{2}\right)$ also see section 3.1.1
Inductive store charging a capacitance using an opening switch
$I_{0}=$ Initial Current
$\boldsymbol{\omega}^{2}=\mathrm{LC}-\left(1 / 4 \mathrm{R}^{2} \mathrm{C}^{2}\right)$
$\boldsymbol{\tau}=\mathrm{RC}$
R = Circuit total Resistance
C = Capacitance to be charged
$\mathrm{V}_{2}(\mathrm{t})=\left(\mathrm{I}_{0} / \omega \mathrm{C}\right) \exp (-\mathrm{t} / 2 \mathrm{tsin} \omega \mathrm{t}$


### 3.4 Energies and Energy Densities

Energy of a capacitor (Joules) $\mathrm{CV}^{2} / 2$
C = Capacitance (F), V = Voltage (Volts) or
Energy of an inductor (Joules) $\quad \mathrm{LI}^{2} / 2$
$\mathrm{L}=$ Inductance ( H ), $\mathrm{I}=$ Current (Amperes)
Energy formulae also give results in joules for units of $\boldsymbol{\mu} \mathrm{F}, \boldsymbol{\mu} \mathrm{H}, \mathrm{kV}, \mathrm{kA}$
Energy density of an E field $\left(\mathrm{J} / \mathrm{m}^{3}\right) \quad \varepsilon \mathrm{E}^{2 / 2}$
$\boldsymbol{\varepsilon}=$ permittivity $(\mathrm{F} / \mathrm{m})$, $\mathrm{E}=$ Elect. field ( $\mathrm{V} / \mathrm{m}$ )
Energy density of a magnetic field ( $\mathrm{J} / \mathrm{m}^{3}$ )
$\mu B^{2 / 2}$
$\boldsymbol{\mu}=$ permeability $(\mathrm{H} / \mathrm{m})$, $\mathrm{B}=$ magnetic field ( T )

### 3.5 Transformer Based Application Circuits

### 3.5.1 Transformer Equivalent Circuit



A number of transformer equivalent circuits exist, and they often differ in their details. In particular, many of the circuits are unable to treat coupling coefficients much less than 1 . For transformers made from sheets, the relative current distribution in the sheet must be assumed to remain fixed in time for this model to be appropriate. In making measurements of equivalent circuit parameters, frequencies used must be close to those in actual use, and the effect of stray components must be quantified. For magnetic core transformers, measurements may need to be made in actual pulsed conditions since permeability can be a strong function of magnetizing current. The calculated turns ratio should be used instead of the counted turns ratio in the calculations below.
$\mathrm{L}_{1}=$ Primary inductance (measured with the secondary open)
$\mathrm{L}_{2}=$ Secondary inductance (measured with the secondary open)
$\mathrm{M}_{1}=$ Mutual inductance referred to primary side
$\mathrm{k}=$ Coupling coefficient
$\mathrm{R}_{1}=$ Primary series resistance
$R_{2}=$ Secondary series resistance

The equivalent circuit parameters are measured or computed as follows. All quantities are referred to the primary side except where indicated by an asterisk:
$N=\left(L_{2} / L_{1}\right)^{1 / 2}$
$\mathrm{L}_{2}=\mathrm{L}_{2}{ }^{*} / \mathrm{N}^{2}$
$L_{p s}=$ primary inductance with the secondary shorted = primary leakage inductance
$L_{s s}{ }^{*}=$ secondary inductance the primary shorted = secondary leakage inductance
$N^{2}=L_{s s}{ }^{*} / L_{p s}$ is a useful consistency check
$\mathrm{R}_{2}=\mathrm{R}_{2}{ }^{*} / \mathrm{N}^{2}$
$\mathrm{k}=\left(1-\mathrm{L}_{\mathrm{ps}} / L_{1}\right)^{1 / 2}=(1-$
$\left.L_{s s} / L_{2}\right)^{1 / 2} M^{*}=k\left(L_{1} L_{2}{ }^{*}\right)^{1 / 2}$
$M_{1}=k\left(L_{1} L_{2}\right)^{1 / 2}$
$I=$ Magnetic path length of core $=2 \mathrm{pr}$ for a toroidal core
$H=$ Magnetization of the core $=\left(\mathrm{N}_{1} \mathrm{l}_{1}-\mathrm{N}_{2} \mathrm{I}_{2}\right) / /$
Energy loss due to magnetizing current $=\mathrm{E}=[\mathrm{VT}]^{2} / 2 \mathrm{~kL}_{1}$ where VT is integrated Voltagetime product.

In general, the capacitances can be ignored in the circuit model unless the circuit impedance is high. Winding resistance (including skin losses) are usually important, as are the inductances.

### 3.5.2 Generalized Capacitor Charging

General capacitor charging relations for arbitrary coupling coefficient, and primary and secondary capacitances. Losses are assumed to be negligible in these formulae

Voltage on charging capacitor $\mathrm{L}_{2}$ :
$V_{2}=k V_{0}\left(\cos s_{1} t-\cos s_{2} t\right) /\left[\left(L_{1} L_{2}\right)^{1 / 2} \mathrm{C}_{2}\left\{\boldsymbol{\omega}_{1}{ }^{4}-2\left(1-2 k^{2}\right) \boldsymbol{\omega}_{1}^{2} \boldsymbol{\omega}_{2}^{2}+\boldsymbol{\omega}_{2}{ }^{4}\right\}^{1 / 2}\right.$
$s_{1}{ }^{2}, s_{2}^{2}=\left(1 /\left(2-2 k^{2}\right)\right)\left\{\boldsymbol{\omega}_{12}+\boldsymbol{\omega}_{12} \pm\left[\boldsymbol{\omega}_{1}{ }^{4}-2\left(1-2 k^{2}\right) \boldsymbol{\omega}_{1}^{2} \boldsymbol{\omega}_{2}^{2}+\boldsymbol{\omega}_{2}\right]^{1 / 2}\right.$
For $\boldsymbol{\omega}_{1}=\boldsymbol{\omega}_{2}=\boldsymbol{\omega}$
$V_{2}(t)=\left(L_{1} / L_{2}\right)^{1 / 2}\left(V_{0} / 2\right)\left[\cos \left(\omega t /(1-k)^{1 / 2}\right)-\cos \omega t /(1+k)^{1 / 2}\right]$
Dual Resonance occurs for $k=0.6$, and $V_{2}$ is maximum at $t=4 / \omega$.
A family of dual resonance solutions exists for lower values of $k$, however, these are of less practical interest

### 3.6 Magnetic Switching

$a=$ inner toroid diameter $(m)$
$b=$ outer toroid diameter $(m)$
$f=$ charge time/discharge time
$E=$ energy in capacitor (joules)
$\delta B=B_{r}+B_{s}$
$B_{r}=$ field at reset (tesla) $B_{s}$
= Saturation field (tesla)
$g=$ packing fraction of magnetic material inside windings
$N=$ number of turns
$\boldsymbol{\tau}=$ charge time of the initial capacitor assuming inductively limited,
capacitor - capacitor charging $(1-$ coswt waveform $)$
$=\pi(L C / 2)^{1 / 2}$ where $L$ is the charging inductance

Minimal volume requirement for magnetic switching is that the relative magnetic permeability
$\mu \gg f^{2}$
$U=p^{3} \times 10^{-7} E^{2} Q /(\delta B g)^{2}$
$=$ Required switch volume $\left(\mathrm{m}^{3}\right)$ for energy transfer between two equal capacitances
Q $=1$ for strip type magnetic switches, or thin annulii
$\mathrm{Q}=\ln (\mathrm{b} / \mathrm{a})[(\mathrm{b}+\mathrm{a}) / 2(\mathrm{~b}-\mathrm{a})]$ for general toroid case
$N=\pi V \boldsymbol{\tau}(b+a) / 2 g \delta B U$

### 4.0 TRANSMISSION LINES AND PULSE FORMING NETWORKS

### 4.1 Discrete Pulse Forming Networks

A variety of pulse forming networks have been developed in order to produce output pulses with a constant, or near constant amplitude for the pulse duration. The ideal physical transmission line may be approximated by an array of equal series inductors and capacitors as shown below. The examples below are optimized 5 element networks which produce the minimum amount of pulse ripple when charged and discharged. These pulse forming networks are discussed in great detail in the work of Glasoe and Lebacz. Negative inductances are not a misprint but reflect the results of calculations.

Five section Guilleman voltage-fed networks. Multiply the printed inductance values by Zt , the capacitances by $t / Z$ where $Z$ is the line impedance, and $t$ is the pulse duration. Zero mutual inductance is assumed in the calculations


### 4.2 Transmission Line Pulse Generators

Ideal pulse line of impedance $Z$ connected to a load of resistance $R$
$\mathrm{V}_{0}=$ open circuit voltage of the pulse
line $\boldsymbol{\tau}=\mathrm{L} /(\mathrm{Z}+\mathrm{R})$
$\mathrm{L}=$ total inductance (switch + connections, etc.)
$I=$ physical length of line for continuous line
$\mathrm{T}=2 / \varepsilon^{1 / 2} / \mathrm{c}$
$\mathrm{n}=$ cycle number
$\boldsymbol{\varepsilon}=$ relative permittivity of the mediumm
$I=V_{0}(1-\exp (-t / \mathbf{\tau})) /(Z+R)$
$V=V_{0} R(1-\exp (-t / \tau) /(Z+R)$
Rise time from . 1 max V to $.9 \mathrm{max} \mathrm{V}=2.2 \mathrm{t}$
The 'plateau' value of load voltage (ignoring rise time effects) changes at time intervals of T . The nth amplitude (where n starts with 0 ) is:
$V(t=n T+T / 2) \simeq V_{0} R(R-Z)^{n} /(R+Z)^{n+1}$
Blumlein response
Ideal Blumlein of impedance $Z$ in each half line, with length / in each half
$\mathrm{L}=$ switch plus connection inductance
$\tau=\mathrm{L} / \mathrm{Z}$
$\mathrm{n}=$ cycle number
$\mathrm{I}_{\mathrm{sw}}=2 \mathrm{~V}_{\mathrm{o}}[1-\exp (-\mathrm{t} / \mathrm{t})] / Z$
$\mathrm{V}=\mathrm{V}_{\mathrm{o}} \mathrm{R}[1-\exp (-\mathrm{t} / \mathrm{t})] /(2 \mathrm{Z}+\mathrm{R})$
$V(t=2 n T+T / 2)=V_{0} R(R-2 Z)^{n} /(R+2 Z)^{n+1}$
$\mathrm{V}(\mathrm{t}=2 \mathrm{nT}+3 \mathrm{~T} / 2)=0$

### 5.0 ELECTRICITY AND MAGNETISM

| L, Inductance (Henries) | C, Capacitance (Farads) |
| :--- | :--- |
| $I$, Length $(\mathrm{m}$, meters $)$ | Z, Impedance $(\boldsymbol{\Omega}$, Ohms) |
| $\mathrm{Z}_{0}=377$ Ohms $=\boldsymbol{\mu}_{0} / \varepsilon_{0}$ | $\boldsymbol{\varepsilon}$, Rel. dielectric Const. |
| $\mathrm{C}=$ Speed of light $=3.0(8) \mathrm{m} / \mathrm{sec}$ | $\boldsymbol{\tau}=2 / \boldsymbol{\varepsilon}^{1 / 2} / \mathrm{c}=$ Output pulse length of a distributed line |

### 5.1 Transmission Line Relationships-General as Applied to Pulse Generation

$C=\varepsilon^{1 / 2} / / \mathrm{Zc}$
$\mathrm{L}=\mathrm{Z} / \boldsymbol{\varepsilon}^{1 / 2} \mathrm{C}$
$(\mathrm{LC})^{1 / 2}=/ \varepsilon^{1 / 2} / \mathrm{C}$
$Z=(L / C)^{1 / 2}$
$C=\varepsilon / 2 Z$
$\mathrm{L}=\mathrm{Z} \mathbf{\tau} / 2$
$\boldsymbol{\tau}=2(\mathrm{LC})^{1 / 2}$

Specific Common Transmission Lines
Coaxial, $a=I D, b=O D, Z=\left(Z_{0} / 2 \pi \varepsilon^{1 / 2}\right) / n(b / a)$
Parallel Wires, $d=$ wire diam, $D=$ Wire center spacing $Z=\left(Z_{0} / \pi \varepsilon^{1 / 2}\right) \cosh ^{-1}(D / d)$
Wire to ground, $\mathrm{d}=$ wire diam, $\mathrm{D}=$ Wire center-ground spacing
$Z=\left(Z_{0} / 2 \pi \varepsilon^{1 / 2}\right) \cosh ^{-1}(2 D / d) \sim\left(Z_{0} / 2 \pi \varepsilon^{1 / 2}\right) / n(4 D / d)$, for $D \gg d$
Parallel Plate, Width w, Separation d, d<w
$Z \simeq Z_{0} d / \varepsilon^{1 / 2}(d+w)$

## Circuit Parameter Formulas

Coaxial Inductor, $b=O D, a=I D L=\left(\mu_{0} / 2 \pi\right) / n(b / a)$
Solenoid,

$$
\begin{array}{ll}
l=\text { solenoid length }(m) & r=\text { solenoid radius }(m) \\
n=\text { turns per meter, } N=/ n & t=\text { solenoid thickness }(m) \\
z=\text { distance between field point and one end of solenoid }(m) \\
V=\text { Volume of the solenoid }\left(m^{3}\right) & I=\text { Current }(A)
\end{array}
$$

Ideal solenoid, where / >> $r$
$\mathrm{L}=\mu_{0} \mathrm{n}^{2} / \pi \mathrm{r}^{2}=1.26 \mathrm{n}^{2} / \pi \mathrm{r}^{2}=4 \mathrm{~N}^{2} \mathrm{r}^{2} / /$ microhenries
Field Energy $=\left(B^{2} / 2 \mu_{0}\right)^{*}$ Volume $=\left(B^{2} / 2 \mu_{0}\right) \pi r^{2} /$
$B=$ mag. field (tesla) $=\mu_{0} \ln =1.26 \times 10^{-6} \mathrm{nl}$
$P=\left(B^{2} / 2 \mu_{0}{ }^{2}\right)^{*}$ Volume ${ }^{*} 4 /(\operatorname{tr})=$ Field Energy $* 4 /(\operatorname{tr})=$ Solenoid Dissipation
Shorter Solenoid or near ends
$B=\left(\mu_{\circ} n l / 2\right)\left[z /\left(z^{2}+r^{2}\right)^{1 / 2}+(l-z) / /\left\{(l-z)^{2}+r^{2}\right\}^{1 / 2}\right]$

## Magnetic Field of a Long Wire

$r=$ distance from wire center $(m), B=\left(\mu_{0} / 2 \pi\right) I / r=200(l($ kiloamps $) / r(c m))$ gauss

## Inductance of a Current Loop

$L=N^{2}(a / 100)\left[7.353 \log _{10}(16 a / d)-6.386\right]$ microhenries $\mathrm{a}=$ mean radius of ring in inches, $\mathrm{d}=$ diameter of winding in inches, and $\mathrm{a} / \mathrm{d}>2.5$

### 5.2 Skin Depth and Resistivity

Skin depth $\boldsymbol{\delta}$ is the depth at which a continous, tangential sinusoidal magnetic field decays to 1/e times the incident field.

$$
\omega=2 \pi f
$$

$\boldsymbol{\mu}=$ permeability of medium
$\rho=$ material resistivity ( $\mathbf{\Omega}-\mathrm{m}$ ); $\boldsymbol{\rho}_{\mathrm{c}}=1.7(-8) \mathbf{\Omega} \mathrm{m}$ (copper)
$\boldsymbol{\delta}=(2 \rho / \boldsymbol{\omega} \boldsymbol{\mu})^{1 / 2}=\left(6.61 / \mathrm{f}^{1 / 2}\right)$ for copper and $\left(8.33 / / \mathrm{f}^{1 / 2}\right)$ for aluminum

Resistance per square $\mathrm{R}_{\mathrm{sq}}$ is the resistance of the surface for a length equal to the width at a given frequency
l= length
w = width
$R=R_{s q} / / w$
$R_{s q}=\rho / \delta=(\omega \mu \rho / 2)^{1 / 2}$
$R_{s q}=2.61(-7) f^{1 / 2}\left(\left(\boldsymbol{\mu} / \mu_{o}\right)\left(\rho / \boldsymbol{p}_{\mathrm{c}}\right)\right)^{1 / 2}$

High frequency resistance of an isolated cylindrical conductor
D = Conductor diameter in inches
Rac = Effective resistance for a CW ac wave
Note that Rac is somewhat smaller for unipolar pulses than for ac.
If $\mathrm{Df}^{1 / 2}\left(\boldsymbol{\mu}_{\mathrm{r}} \boldsymbol{\rho}_{\mathrm{c}} / \boldsymbol{\rho}\right)^{1 / 2}>40$ :
$R_{\mathrm{ac}} \simeq\left(\mathrm{f}^{1 / 2} / \mathrm{D}\right)\left(\mathbf{m}_{\mathrm{r}} \mathbf{\rho} / \boldsymbol{\rho}_{\mathrm{c}}\right)^{1 / 2} \times 10^{-6} \mathrm{ohms} / \mathrm{ft}$.
If $\mathrm{Df}^{1 / 2}\left(\boldsymbol{\mu}_{\mathrm{r}} \boldsymbol{\rho}_{\mathrm{c}} / \mathbf{\rho}\right)^{1 / 2}<3$, then $\mathrm{Rac}_{\mathrm{ac}} \sim \mathrm{R}_{\mathrm{dc}}$

### 5.3 Field Enhancement Functions in Various Geometries

Cylindrical Geometry where X is the distance between two conductors, and r is the radius of the smaller conductor.

Cylindrical Field Enhancement


Field enhancement factor for cylindrical configurations. Upper: coaxial line, Intermediate : conducting cylinder adjacent to a plane. Lower: two parallel conducting cylinders

## Maximum field strength equations for Cylindrical Geometry:

$\mathrm{b}=$ outer cylinder radius
$\mathrm{E}=\mathrm{V} /(\mathrm{rln}(\mathrm{b} / \mathrm{r})) \quad$ Concentric cylinders
$E=V\left(D^{2}-4 r^{2}\right) /\left[2 r(D-2 r) \ln \left\{(D / 2 r)+\left((D / 2 r)^{2}-1\right)^{1 / 2}\right\}\right]$
where $D=X+2 r$ for parallel cylinders, and $D=2 X+2 r$ for a cylinder spaced $X$ from a uniform ground plane and parallel to it.

Semicylinder on a plane $E_{m}=2 E$ where $E$ is the applied electric field

Spherical Field Enhancement


Spherical field enhancement including concentric spheres (upper) sphere-plane (middle) and adjacent spheres (lower).
Maximum field strength equations for Spherical geometry.
$R=$ outer sphere radius
$r=$ inner sphere radius
$E=V R / r(R-r) \quad$ Concentric spheres
$\left.\mathrm{E}=\mathrm{V}\left[(\mathrm{X} / \mathrm{r})+1+((\mathrm{X} / \mathrm{r})+1)^{2}+8\right)^{1 / 2}\right] / 4 \mathrm{X} \quad$ Equal spheres spaced X
$\left.\mathrm{E}=\mathrm{V}\left[(2 \mathrm{X} / \mathrm{r})+1+((2 \mathrm{X} / \mathrm{r})+1)^{2}+8\right)^{1 / 2}\right] / 8 \mathrm{X}$ Sphere of radius r spaced X from a ground plane
Hemisphere on a plane in a uniform field of amplitude E: $\quad E_{m}=3 E$

### 6.0 MATERIALS PROPERTIES

The dielectric properties of gases and liquids are understood (empirically), and are presented as such. The typical values of dielectric strength for solids are an exception to this understanding. Solid breakdown depends on preparation, pulse life requirements, and the medium in which the solid is contained. The values quoted in this document for solid breakdown actually refer to long term working strength, and must be considered to be of limited value. Note that in general, the dielectric strength of all materials decreases with increasing sample thickness. $\mathbf{e}$ is the relative permittivity below, and tan dis the energy loss per cycle.

### 6.1 Solid Dielectric Properties

| Material | Diel. Const.$60 \text { Hz. }$ |  | Diel. Const. 1 MHz . |  | Diel. <br> Strength* <br> V/mil |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\varepsilon$ | $\tan \boldsymbol{\varepsilon}$ | $\varepsilon$ | $\tan \boldsymbol{\varepsilon}$ |  |
| Aluminum Oxide | 8.80 | 3.3(-4) | 8.80 | 320 | 320 |
| Barium Titanate | 1250 | 0.056 | 1143 | 0.0105 | 75 |
| Soda-Borosilicate Glass | 4.97 | ----- | 4.84 | 3.6(-3) | 400 |
| Epoxy (Epon RN-48) | 4.50 | 0.05 | 3.52 | 0.0142 | 800 |
| Polycarbonate | 3.17 | 0.009 | 2.96 | 0.01 | 400 |
| Acrylic | 4.0 | 0.016 | 2.55 | 0.009 | 400 |
| Polyimide | 3.4 | 0.002 | 3.4 | 0.003 | 570 |
| Polyvinyl Chloride | 3.20 | 0.0115 | 2.88 | 0.016 | 400 |
| PTFE (Teflon) | 2.10 | <5(-4) | 2.10 | <2(-4) | 550 |
| Polyethylene | 2.26 | <2(-4) | 2.26 | <2(-4) | 450 |
| Polypropylene | 2.55 | <5(-4) | 2.55 | <5(-4) | 650 |
| Paper | 3.30 | 0.010 | 2.99 | 0.038 | 200 |

*Typical DC values for .10 inch thick samples

### 6.2 Gas Properties

Gas breakdown, DC to approximately 1 microsecond
$\mathrm{E}=24.5 \mathrm{p}+6.7\left(\mathrm{p} /\right.$ Reff $^{1 / 2} \mathrm{kV} / \mathrm{cm}$. Air
$R_{\text {eff }}=.115 R$ for spheres, and $.23 R$ for cylinders, and the gap distance for planar geometries, where $p$ is the pressure in atmospheres

Resistive phase duration of an air arc
$t=88 p^{1 / 2} /\left(Z^{1 / 3} E^{4 / 3}\right)$ nanoseconds
where p is the pressure in atmospheres, E is the electric field in $\mathrm{MV} / \mathrm{m}$, and Z is the characteristic impedance of the circuit.

Relative electric strengths:
Relative breakdown field compared to air

| ===================================== |  |
| :--- | :---: |
| Air | 1.0 |
| Nitrogen | 1.0 |
| SF6 | 2.7 |
| Hydrogen | 0.5 |
| $30 \%$ SF $_{6}, 70 \%$ air (by volume) | 2.0 |

## Paschen's Law

Under most circumstances, the breakdown of gases is a function of the product of pressure (p) and gap length (d) only, where this function depends on the gas.
$V=f(p d)$
The breakdown strength of a gas is monotonic decreasing below a specified value of $\mathrm{pd}=$ (pd)crit and monotonic increasing above that value. The values of (pd)crit and the breakdown voltage at that value of pd are given below:

Gas

| $\mathrm{pd}_{\text {crit }}$ | (pd cerit) <br> (Torr-cm) |
| :--- | :--- |
| (Volts) |  |


| ==================================== |  |  |
| :--- | :--- | :--- |
| Air | 0.567 | 327 |
| Argon | 0.90 | 137 |
| Helium | 4.0 | 156 |

760 Torr = 1 standard atmosphere

### 6.3 Liquid Breakdown

```
\(t=\) time that the pulse is above \(63 \%\) of peak voltage (msec)
\(A=\) Stressed area \(\left(\mathrm{cm}^{2}\right)\)
d = gap between electrodes
\(\mathrm{E}=\) Electric field (MV/cm)
```


## Pulse Breakdown of Liquids

Transformer Oil
$\mathrm{E}_{+}=.48 /\left(\mathrm{t}^{1 / 3} \mathrm{~A}^{.075}\right) \quad$ (Positive Electrode)
$\mathrm{E}-=1.41 \mathrm{E}+\boldsymbol{\alpha} \quad$ (Negative Electrode)
$\left.\boldsymbol{\alpha}=1+.12\left[\mathrm{E}_{\max } / \mathrm{E}_{\text {mean }}\right)-1\right]^{1 / 2}$
Note: The above formulae do not apply if a DC pre-stress is applied across the gap

## Water

$\mathrm{E}_{+}=.23 /\left(\mathrm{t}^{1 / 3} \mathrm{~A}^{.058}\right) \quad$ (Positive Electrode)
$E_{-}=.56 /\left(\mathrm{t}^{1 / 3} \mathrm{~A}^{.070}\right) \quad$ (Negative Electrode)

## Resistive phase rise time of a switch

$\boldsymbol{\tau}_{r}=5 \boldsymbol{\rho}^{1 / 2} / Z^{1 / 3} E^{4 / 3}$ where $\boldsymbol{\rho}\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ is the density of the liquid, $Z$ is the impedance of the circuit in ohms, and $E$ is the electric field in $\mathrm{MV} / \mathrm{cm}$. This formula is thought to work for oil, water, and gas switches.

## General comments on breakdown of transformer oil

Pulse power operation (typical) 100-400 kV/cm for pulsed operation with no DC prestress. The exact value is dependent on the oil, and field enhancements. For conservative DC operation $40 \mathrm{kV} / \mathrm{inch}$ is generally a reliable guideline. This value generally allows the user to ignore field enhancements and dirt when designing the DC system. If carbon streamers form in the oil during a pulse, these values no longer apply. Filtration and circulation are required in oil to avoid carbon build-ups. $40 \mathrm{kV} / \mathrm{cm}$ is a reliable number for careful DC design.

### 6.4 Vacuum Insulation and Surface Flashover

We assume in this section that the pressure is below $10^{-4}$ Torr, and note that variations due to the residual gas pressure are observed at pressures as low as $10^{-6}$ Torr.
$\mathrm{d}=$ individual insulator length (cm.)
A = insulator area ( $\mathrm{cm}^{2}$ )
$\mathrm{t}=$ pulse duration or pulse train duration ( msec )

## Pulsed 45 degree acrylic insulators in vacuum

$E=175 /\left(t^{1 / 6} A^{1 / 10}\right) \mathrm{kV} / \mathrm{cm}$. typical for 1-2" long insulators, and more than 5 insulators
$E=33 /\left(\mathrm{t}^{1 / 2} \mathrm{~A}^{1 / 10} \mathrm{~d}^{0.3}\right) \mathrm{kV} / \mathrm{cm}$ for bipolar pulses
DC Flashover
Material Electric field (kV/cm.)

| ================================== |  |
| :--- | :--- |
| Glass | $18 / d^{1 / 2}$ |
| Teflon | $22 / d^{1 / 2}$ |
| Polystyrene | $35 / d^{1 / 2}$ |

## Vacuum breakdown

Vacuum breakdown between parallel electrodes depends on surface preparation, pulse length electrode history, and possibly gap length, as well as material type.

We list typical values below primarily in order to give the reader an ordering of material strength. The typical voltage at which the data below is applicable is 500 kV .

Material Pulse Breakdown (kV/cm.) 100 ns .

| Aluminum | 290 |
| :--- | :--- |
| Graphite (Poco) | 175 |
| Lead | 170 |
| Molybdenum | 460 |
| Stainless Steel | 300 |
| Velvet | $20-50$ |

A variation of breakdown strength with gap length of $\mathrm{d}^{-0.3}$ may be inferred from some data, however this effect is more pronounced in DC high voltage breakdown

### 6.5 Conductor Properties

Conductivities of Conductors

| Material | Density | Resistivity(20C) <br> $\left(\mathrm{gm} / \mathrm{cm}^{3}\right)$ | Ht. Cap. <br> $\left(10^{-6} \mathrm{ohm}-\mathrm{cm}\right)$ | Temp. Coef. <br> $(\mathrm{J} / \mathrm{gmC})$ |
| :--- | :--- | :--- | :--- | :--- |
|  | $(1 / \mathrm{C})$ |  |  |  |


| Aluminum | 2.70 | 2.62 | . 946 | 0.0039 |
| :---: | :---: | :---: | :---: | :---: |
| Beryllium | 1.85 | 35 | 1.78 | 0.0042 |
| Bismuth | 9.80 | 115 | 0.123 | 0.004 |
| Brass (66Cu,34Zn) | 8.40 | 3.9 | 0.418 | 0.002 |
| Chromium | 7.19 | 2.6 | 0.460 |  |
| Copper | 8.96 | 1.72 | 0.418 | 0.0039 |
| Graphite (typical) | 2.25 | 1400 | 0.894 | -0.0005 |
| Gold | 19.3 | 2.44 | 0.130 | 0.0034 |
| Indium | 7.31 | 9 | 0.238 | 0.0050 |
| Iron | 7.87 | 9.71 | 0.452 | 0.0057 |
| Lead | 11.34 | 21.9 | 0.126 | 0.004 |
| Magnesium | 1.74 | 4.46 | 1.04 | 0.004 |
| Nichrome (typical) | 100 | ----- | ----- | 0.00017 |
| Nickel | 8.9 | 6.9 | 0.268 | 0.0047 |
| Silicon | 2.4 | 85,000 | 0.736 | ------ |
| Silver | 10.5 | 1.62 | 0.234 | 0.0038 |
| Stainless Steel | 7.90 | 90 | ----- | ------ |
| Steel (.5\%C) | 7.90 | 13-22 | 0.520 | 0.003 |
| Tantalum | 16.6 | 13.1 | 0.151 | 0.003 |
| Tin | 7.3 | 11.4 | 0.226 | 0.0042 |
| Titanium | 4.54 | 47.8 | 0.594 | ------ |
| Tungsten | 19.3 | 5.48 | 0.142 | 0.0045 |

### 6.5.1 Wire Data--Standard Sizes of Copper Wire

| AWG B\&S DIAM. GAUGE (MILS) |  | $\begin{aligned} & \text { OHMS PER } \\ & 1000 \mathrm{FT} \end{aligned}$ | $\begin{aligned} & \text { LB. PER } \\ & 1000 \text { FT } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 0000 | 460 | . 049 | 640 |
| 000 | 410 | . 062 | 509 |
| 00 | 365 | . 078 | 403 |
| 0 | 324 | . 099 | 318 |
| 1 | 289 | . 124 | 253 |
| 2 | 257 | . 157 | 200 |
| 3 | 229 | . 198 | 159 |
| 4 | 204 | . 249 | 126 |
| 5 | 182 | . 313 | 100 |
| 6 | 162 | . 395 | 79.4 |
| 7 | 144 | . 500 | 62.8 |
| 8 | 128 | . 633 | 49.6 |
| 9 | 114 | . 798 | 39.3 |
| 10 | 102 | . 997 | 31.5 |
| 11 | 90.7 | 1.26 | 24.9 |
| 12 | 80.8 | 1.59 | 19.8 |
| 13 | 72.1 | 1.99 | 15.7 |
| 14 | 64.1 | 2.52 | 12.4 |
| 15 | 57.1 | 3.18 | 9.87 |
| 16 | 50.8 | 4.02 | 7.81 |
| 17 | 45.3 | 5.05 | 6.21 |
| 18 | 40.3 | 6.39 | 4.92 |
| 19 | 35.9 | 8.05 | 3.90 |
| 20 | 31.2 | 10.7 | 2.95 |
| 21 | 28.5 | 12.8 | 2.46 |
| 22 | 25.4 | 16.1 | 1.95 |
| 23 | 22.6 | 20.3 | 1.55 |
| 24 | 20.1 | 25.7 | 1.22 |
| 25 | 17.9 | 32.4 | . 970 |
| 26 | 15.9 | 41.0 | . 765 |
| 27 | 14.2 | 51.4 | . 610 |
| 28 | 12.6 | 65.3 | . 480 |

### 6.6 Magnetic materials

| Material | Sat. flux kG $B$ s | ```Res. Flux kG B``` | Init. perm. DC <br> $\mathbf{m}_{\mathrm{i}}$ | Max. perm DC m | . Resistivity ohm-cm r |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Metglas |  |  |  |  |  |
| 2605SC | 16.1 | 14.2 | 8,000 | 300,000 | 142(-6) |
| 2605CO | 18.0 | 16.0 | 5,000 | 250,000 | 160(-6) |
| 3\% Si-Fe | 16.5 | 14-15 | 500 | 25,000 | 50(-6) |
| Permalloy | 7.5 | 6.0 | 20,000 | 150,000 | 45(-6) |
| 50\% Ni-Fe | 16.0 |  | 2,500 | 25,000 | 45(-6) |
| NiZn Ferrite CN20* | 3.8 | 2.7 | 800 | 4,500 | 1(6) |
| MnZn Ferrite |  |  |  |  |  |
| 3C80** | 5.0 | 1.6 | 2,000 |  | 4.8 |
| MN80* | 5.0 | 2.5 | 1,500 | 5,000 | 200 |

Note that the data above are applicable for low frequencies, and the performance at higher frequencies is dependent on frequency. Metal materials must be wound in thin insulated tapes for most pulse power applications. * Ceramic Magnetics ** Ferroxcube

### 6.6 Components

### 6.6.1 Capacitors

$\mathrm{N}=$ number of pulses to failure
$E=$ Electric field in application
$\mathrm{V}_{\mathrm{b}}=\mathrm{DC}$ breakdown voltage
$\mathrm{d}=$ dielectric thickness
$Q=$ circuit quality factor
$\boldsymbol{\beta}=$ thickness exponent, typically less than 3
$\mathrm{V}_{\mathrm{r}}=$ reversal voltage
$N \alpha\left(E d / V_{b}\right)^{-8} d^{-\beta} Q^{-2.2}$ for plastic capacitors
$\mathrm{Na}\left(\mathrm{Ed} / \mathrm{V}_{\mathrm{b}}\right)^{-12} \mathrm{Q}^{-2.2}$ for ceramic capacitors
$V_{r}=1-\pi 2 Q$

Notes: Barium Titanate capacitors--unless specially prepared--vary in capacitance by about a factor of 2 over their range of voltage utilization

Mica capacitors have an excellent combination of dissipation factor, and low change in value under voltage and temperature stress, but only at high cost.

Paper and plastic capacitors can have significant internal inductance and resistance, and these quantities must be ascertained in any critical application. In practice it is nearly impossible to discharge any paper or plastic capacitor in less than 100 ns, and many capacitors may take much longer to discharge.

### 6.6.2 Resistors

General comments on performance under pulse power conditions.
Carbon composition resistors have excellent performance in voltage and power handling, but may have resistance variations with voltage of $2-50 \%$ depending on type, history, etc.

Metal film resistors must be specially designed for high voltage and pulse power use. The pulse energy handling capability of film resistors is generally inferior to that of bulk resistors due to the relatively small mass of the current carrying component.

Liquid resistors such as water/copper sulphate, etc, are subject to variation in resistivity with time. The preferred method for measuring the resistance of these components is with a pulsed high voltage (measuring current for a known voltage). DC measurments at low voltage can often be wrong by factors of 2 or 3 .

### 7.0 APPLICATIONS

### 7.1 Intense Electron and Ion Beam Physics

Space charge limited electron emission current, or 'Child-Langmuir' current density
$\mathrm{V}=$ Voltage applied in MV
$\mathrm{d}=$ gap between anode and cathode in cm .
$\mathrm{J}_{\mathrm{s}}=$ Current density $=2.34 \mathrm{~V}^{3 / 2} / \mathrm{d}^{2} \mathrm{kA} / \mathrm{cm}^{2}$ for $\mathrm{V}<.5 \mathrm{MV}$
$J_{s}=2.7\left[(\mathrm{~V} / 0.51+1)^{1 / 2}-0.85\right]^{2} / \mathrm{d}^{2} \mathrm{kA} / \mathrm{cm}^{2}$ for $\mathrm{V}>.5 \mathrm{MV}$
Bipolar flow in an anode-cathode gap where the anode is also a source of space charge limited ions
$\mathrm{J}=1.84 \mathrm{Js}(\mathrm{V}<.5 \mathrm{MV})$
$\mathrm{J}=2.14 \mathrm{~J} \mathrm{~s}(\mathrm{~V}>.5 \mathrm{MV})$
Typical thermionic emitter data

| Material | efficiency <br> $(\mathrm{mA} / \mathrm{watt})$ | Typ. J <br> $\left(\mathrm{amps} / \mathrm{cm}^{2}\right)$ | Temperature <br> (Kelvin) | hot R/cold R <br> $\mathrm{R}=$ Resistance |
| :--- | :--- | :--- | :--- | :--- |
| ============================================================= |  |  |  |  |
| Tungsten | $5-10$ | $.25-.7$ | 2550 | $14 / 1$ |
| Th-W | $40-100$ | $0.5-3.0$ | 2000 | $10 / 1$ |
| Tantalum | $10-20$ | $0.5-1.2$ | 2450 | $6 / 1$ |
| Oxide | $50-150$ | $0.5-2.5$ | 1100 | ---- |
| Dispenser | $100-2000$ | $1.0-25$ | 1400 | ----- |
| LaB6 | $200-500$ | $1.0-60$ | 1970 | ---- |

## Vacuum beam propagation

## Space charge limiting current

$$
\begin{aligned}
& b=\text { beam conducting drift tube diameter } \\
& \text { a = beam outer diameter } \\
& f=\text { ratio of ion to electron densities } \\
& g=\ln (b / a) \text { for annular beams } \\
& =1 / 2+\ln (b / a) \text { for solid beams } \\
& \alpha=1+e \mathrm{ea} \overline{\mathrm{~B}} / \mathrm{mc}=1+\mathrm{a} \overline{\mathrm{~B}} \mathrm{~B} / 1.7 \\
& \delta B=\text { change in magnetic field ( } k G \text { in numerical formula) } \\
& \text { giving rise to rotation } \\
& Y=1+V / 0.51=1 /\left(1-\beta^{2}\right)^{1 / 2}=\text { relativistic } \\
& \text { factor } \beta=\mathrm{v} / \mathrm{c}=\text { normalized beam velocity } \\
& \mathrm{l}_{\mathrm{o}}=4 \mathrm{mmc} / \mu_{\mathrm{o}} \mathrm{e}=17,000 \text { amperes } \\
& \mathrm{I}<17\left(\mathrm{Y}^{2 / 3}-1\right)^{3 / 2} /(1-\mathrm{f}) \mathrm{g} \text { kiloamperes } \\
& K=\left(2 I / 17 \beta^{2} \mathbf{Y}\right)\left[1 / \mathbf{Y}^{2}-f\right] \\
& \mathrm{a}=\mathrm{dr} / \mathrm{dz} \\
& \mathrm{a}_{\mathrm{o}}=\text { initial beam radius } \\
& r / a_{o}=\exp \left(a_{2} / 2 K\right) \\
& r / a_{o}=\exp \left(a^{2} / 2 K\right)
\end{aligned}
$$

## Beam equilibrium condition

## $\mathrm{I}<0.7 \beta_{p} \mathrm{~B}^{2} \mathrm{a}^{2} \boldsymbol{\gamma} \mathrm{kA}$

$\beta_{p}$ is the component of $\beta$ in the direction of beam propagation, $B$ is in $k G$, and $a$ is in $c m$.
Magnetic field energy required to focus a beam in equilibrium (note that this may not assure stability)
$\mathrm{k}_{1}=$ ratio of field coil radius to beam radius
$\mathrm{k}_{2}=$ ratio of field to minimum field
$\mathrm{k}_{3}=$ ratio of field energy inside coil radius to field energy outside coil radius
$t=$ length of field region (cm.)
$\mathrm{E}=$ Energy of magnetic field (joules)
$E=.036 I k_{1}{ }^{2} k_{2}{ }^{2} k_{3} / b_{p} g$

## Beam rotation

$$
\boldsymbol{\omega}_{\mathrm{c}}=2 \pi \mathrm{f}_{\mathrm{c}}=\mathrm{eB} / \mathbf{y m c}=17 \mathrm{~B} / \mathbf{y} \text { Ghz. = cyclotron angular frequency }
$$

where $B$ is in $k G$

$$
r_{L}=\boldsymbol{\beta} / \omega_{c}=1.7\left(\mathbf{y}^{2}-1\right)^{1 / 2} / \mathrm{B}
$$

cm. Cusp Condition

$$
\begin{aligned}
& \delta B=B_{\text {initial- }} \mathrm{B}_{\text {final }} \text { in kilogauss } \\
& r<3.4\left(\mathrm{y}^{2}-1\right)^{1 / 2} / \delta B
\end{aligned}
$$

## Magnetic Insulation

$$
\begin{aligned}
& d=\text { anode-cathode gap in cm. for planar geometry }= \\
& \left(b^{2}-a^{2}\right) / 2 a \text { in cylindrical geometry }(b=O D, a=I D) \\
& B>(1.7 / d)\left(y^{2}-1\right)^{1 / 2} k G
\end{aligned}
$$

Self magnetic insulation
Minimum current $=\mathrm{I}=8.5\left(\mathrm{Y}^{2}-1\right)^{1 / 2} / \ln (\mathrm{b} / \mathrm{a})$

$$
\text { kiloamps }=\left(\mathrm{I}_{\mathrm{o}} / 2\right)\left(\mathbf{r}^{2}-1\right)^{1 / 2} / \ln (\mathrm{b} / \mathrm{a})
$$

### 7.2 Electron Beam/Matter Interaction

## Stopping Power and Range

Note that electron beams do not have a well defined stopping point in material. The CSDA range follows the path of an electron ignoring scattering, and is the longest distance an electron can physically travel. The practical range is the linear extrapolation of the depthdose curve and indicates a point where the electron flux is a few percent of the incident flux. Electron ranges and stopping powers are approximately proportional to the electron density in the medium.

| Electron energy | CSDA Range in Al. | Practical Range in Al. <br> $(\mathrm{MeV})$ |
| :--- | :--- | :--- |
| $\mathrm{gm} / \mathrm{cm}^{2}$ | $\mathrm{~g} / \mathrm{cm}^{2}$ |  |


| .1 | .018 | 0.009 |
| :--- | :--- | :--- |
| .5 | .25 | 0.16 |
| 1.0 | .61 | 0.42 |
| 2.0 | 1.33 | 0.95 |
| 5.0 | 3.3 | 2.40 |
| 10.0 | 6.1 | 5.0 |

Radiation production with electron beams
$100 \mathrm{ergs} / \mathrm{gram}=1$ Rad $10 \mathrm{Joules} / \mathrm{gram}=1 \mathrm{MRad}$
For 1-10 MeV Aluminum, $1 \mathrm{mCoulomb} / \mathrm{cm}^{2} \simeq 0.2$ megarads on average over the range
X-ray production efficiency
$\mathrm{V}=$ beam energy in megavolts
$\mathrm{Z}=$ Target atomic number
I = Beam current in kiloamperes
$(\mathrm{X}$-ray energy total/Beam energy $)=7(-4) \mathrm{ZV}$
Dose rate $\mathrm{D}(\mathrm{rads} / \mathrm{sec})$ at 1 meter directly ahead of the beam
$D=1.7(6) I^{2.65}$ for $Z=73$
Blackbody Radiation Law
T = Temperature (Kelvin)
$\varepsilon=$ Emissivity of surface
Radiation flux $=5.67(-8) \varepsilon \mathrm{T}^{4} \mathrm{~W} / \mathrm{m}^{2}$

### 7.3 High Power Microwaves

$f(c)=$ frequency (of cutoff)
c= Speed of light
$\boldsymbol{\lambda}_{\mathrm{g}}=$ waveguide wavelength
$\omega=2 \pi f$
$k=2 \pi / \lambda g$
Frequency Band Designations:

| Tri-Service F(Ghz.) | World War II Designation | F(Ghz.) | Designation | de |
| :---: | :---: | :---: | :---: | :---: |
| 0.0-. 25 | A | .003-.030 | HF |  |
| .25-. 50 | B | .030-. 300 | VHF |  |
| .50-1.0 | C | .300-1.12 | UHF |  |
| 1.0-2.0 | D | 1.12-1.76 | L | WR650 |
| 2.0-3.0 | E | 1.76-2.60 | LS | WR430 |
| 3.0-4.0 | F | 2.60-3.95 | S | WR284 |
| 4.0-6.0 | G | 3.95-5.89 | C | WR187 |
| 6.0-8.0 | H | 5.89-8.20 | XN | WR137 |
| 8.0-10.0 | I | 8.20-12.9 | X | WR90 |
| 10.0-20.0 | J | 12.9-18.0 | Ku | WR6 |
| 20.0-40.0 | K | 18.0-26.5 | K | WR42 |

Waveguide Relations
$\mathrm{f}^{2}=\mathrm{f}_{\mathrm{c}}{ }^{2}+\left(\mathrm{c} / \boldsymbol{\lambda}_{\mathrm{g}}\right)^{2}$
Rectangular Waveguide, dimensions $a, b, a>b$

$$
\boldsymbol{\lambda}_{\mathrm{g}}=2 \mathrm{a} \text { TE01, } \boldsymbol{\lambda}_{\mathrm{g}}=2 \mathrm{a} /\left(1+(\mathrm{a} / \mathrm{b})^{2}\right)^{1 / 2} \quad \text { TE11, } \boldsymbol{\lambda}_{\mathrm{g}}=2 \mathrm{a} /\left(1+(\mathrm{a} / \mathrm{b})^{2}\right)^{1 / 2} \mathrm{TM} 11,
$$

Circular Waveguide, dimension $\mathrm{a}=$ radius
$\lambda_{g}=1.640 a$ TE01
$\lambda_{g}=2.613 \mathrm{a}$ TM01
$\lambda_{g}=3.412 \mathrm{a}$ TE11
$\boldsymbol{\lambda}_{\mathrm{g}}=1.640 \mathrm{a}$ TM11

### 7.4 Railguns

## Capacitor - Driven Rail Gun Circuit



Voltage: $\left(L_{0}+L_{G}\right) d^{2} q / d t^{2}+\left(R_{0}+R_{G}+\left(d L_{G} / d x\right) v\right) d q / d t+q / C=V_{0}$
Eq. of Motion: $\left(m_{p}+\left(d m_{a} / d x\right) x\right) d^{2} x / d t^{2}=(1 / 2)\left(d L_{G} / d x\right)(d l / d t)^{2}-\left(d m_{a} / d x\right)(d x / d t)^{2}$
Electrode pressure: $\quad P=\left.(1 / 2)\left(\left(d L_{G} / d x\right) / A\right)\right|^{2}$
for $\mathrm{dm} / \mathrm{dx}=0, \mathrm{I}=$ constant: $\mathrm{v}=\left[(\mathrm{dL} / \mathrm{dx}) \mathrm{Ix} / \mathrm{m}_{\mathrm{P}}^{\mathrm{A}}\right]^{1 / 2}$

$$
R_{G}=R_{G o}+\left(d R_{G} / d x\right) x
$$

for $m=0, \quad I=\operatorname{lexp}\left(-a t s i n w t, L_{G}=L_{G o}+L_{G X}\right.$
$C=$ driver capacitance
$R_{0}=$ driver resistance (fixed)
$\mathrm{L}_{\mathrm{o}}=$ driver inductance (fixed)
$\mathrm{q}=$ charge
$\mathrm{A}=$ cross-sectioned gun area
$\mathrm{dR} / \mathrm{dx}=$ gun longitudinal resistance gradient
$\mathrm{dL} / \mathrm{dx}=$ gun longitudinal inductance gradient
$x=$ Longitudinal distance
$\mathrm{v}=$ Longitudinal projectile relocity
$\mathrm{m}_{\mathrm{p}}=$ projectile mass
$d m_{a} / \mathrm{dx}=$ longitudinal air mass gradient

Ablation rate constants (Jerall V. Parker, Proceedings at the IEEE 3rd Symposimm on Electromagnetic Launch Technology, Austin, TX, 1988)

## Gun Mode

Material Ablation Vaporization Erosion (gas - liquid)

| ============================================== |  |  |  |
| :--- | :--- | :--- | :--- |
| Copper | $28 \mathrm{~g} / \mathrm{MJ}$ | $118 \mathrm{~g} / \mathrm{MJ}$ | $143-1630 \mathrm{~g} / \mathrm{MJ}$ |
| Tungsten | 88 | 160 | $185-1575$ |
| Polyethylene | 3.4 | 25 | $500-6,800$ |
| Lexan | 5.6 | 40 |  |
| G-10 | 6.7 | 40 |  |

### 8.0 DIAGNOSTICS

### 8.1 Sensitivity of an Unintegrated Square Current Loop

$\mathrm{b}=$ outer conductor distance to current source center(m)
$\mathrm{a}=$ inner conductor distance to current source center( m )
I = length of current loop(m) parallel to current axis
$\mathrm{N}=$ number of turns in the current loop
$V_{\text {out }}=\left(\mu_{0} N / 2 \pi\right) / n(b / a)(d / / d t)$
Integrated using a passive RC integrator

$$
\begin{aligned}
& V_{\text {out }}=\left(\mu_{0} N / n(b / a) / 2 \pi R C\right) \text { ) } \\
& =2 N /(\ln (\mathrm{b} / \mathrm{a}) / \mathrm{RC}) \mathrm{I} / \text { is in } \mathrm{cm} ., \mathrm{I} \text { in } \mathrm{kA}, \mathrm{RC} \text { in } \mu \mathrm{sec} \mathrm{R} \\
& =\text { resistance of the RC integrator } \\
& \mathrm{C}=\text { capacitance of the RC integrator } \\
& \text { RC product in seconds or microseconds as appropriate above } \\
& \text { I = current to be measurement }
\end{aligned}
$$

### 8.2 Rogowski Coil

The Rogowski coil consists of N turns wound on a form circular in shape evenly along the major circumference. Each turn has an area A. The major circumference has a radius $\mathbf{r}$, and the output is independent of the relative position of the current flow as long as the winding source is more than 2 turn spacings away from the current source.

$$
\mathbf{r}=\text { major radius of the Rogowski coil }
$$

$$
\begin{aligned}
V_{\text {out }} & =\left(\mu_{0} \mathrm{NA} / 2 \pi r\right) \mathrm{dl} / \mathrm{dt} & & \text { Unintegrated } \\
V_{\text {out }} & =\left(\mu_{0} \mathrm{NA} / 2 \pi r \mathrm{RC}\right) \mathrm{I} & & \text { Integrated } \\
& =(2 \mathrm{NA} / \mathrm{rRC}) \mathrm{I} & & \text { integrated } \mathrm{A}\left(\mathrm{~cm}^{2}\right), \mathbf{r}(\mathrm{cm}), \mathrm{RC}(\mu \mathrm{sec}), \mathrm{I}(\mathrm{kA}) \\
& =(12.63 \mathrm{nA} / \mathrm{RC}) I & & \text { integrated } \mathrm{A}\left(\mathrm{~cm}^{2}\right), \mathrm{RC}(\mu \mathrm{sec}), \mathrm{n}\left(\mathrm{~cm}^{-1}\right)
\end{aligned}
$$

### 8.3 Current Transformer

Given appropriate frequency response in the core, a current transformer will give linear output over a wide range of time scales and currents.
$R=$ total terminating resistance of the measurement circuit
$b=$ od of square core
a = id of square core $l=$
length of square core
ठB = saturation magnetization of core
$\mathrm{N}=$ number of turns
$\mu_{\mathrm{o}}=$ Permeability ( $\mathrm{H} / \mathrm{m}$ )
$V_{\text {out }}=(R / N) I$
$Z=R / N^{2}=$ insertion impedance of the current transformer
$\boldsymbol{\tau}=\boldsymbol{\mu} \mathrm{N}^{2} / \ln (b / a) / R=$ exponential decay time of signal
$I_{\max } \tau_{\max }=\mathrm{N}^{2}(\mathrm{~b}-\mathrm{a}) / \overline{\mathrm{B}} / \mathrm{R}$
The risetime of current transformers is generally determined empirically

### 8.4 Attenuators

T-pad type attenuators are commonly used in fixed impedance (typically 50 ohm) systems. We list the general equation for this type of attenuator, and several standard values.
$\mathrm{Z}=\mathrm{characteristic}$
$\mathrm{K}=$ attenuation factor (>1)
= voltage out/voltage in
$R_{1}=Z[1-2 /(K+1)]$
$R_{2}=2 Z K /\left(K^{2}-1\right) A=20 \log _{10}(K)=10 \log _{10}$ (Power
 $\mathrm{in} /$ Power out) $=$ attenuation in db

50 ohm attenuator combinations

| K | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ |
| :--- | :--- | :--- |

$2 \quad 16.7 \quad 66.7$
$5 \quad 33.3 \quad 20.8$
$10 \quad 43.9 \quad 10.1$

### 9.0 MECHANICAL DATA

### 9.1 Coarse Screw Threads

| Size | Thds. per inch | Major diam. (inches) | Minor diam. (inches) | Lead (deg.) | (min.) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 64 | 0.073 | 0.056 | 4 | 31 |
| 2 | 56 | 0.086 | 0.067 | 4 | 22 |
| 3 | 48 | 0.099 | 0.076 | 4 | 26 |
| 4 | 40 | 0.112 | 0.085 | 4 | 45 |
| 5 | 40 | 0.125 | 0.098 | 4 | 11 |
| 6 | 32 | 0.138 | 0.101 | 4 | 50 |
| 8 | 32 | 0.164 | 0.130 | 3 | 58 |
| 10 | 24 | 0.190 | 0.145 | 4 | 39 |
| 12 | 24 | 0.216 | 0.171 | 4 | 1 |
| $1 / 4$ | 20 | 0.250 | 0.196 | 4 | 11 |
| 5/16 | 18 | 0.313 | 0.252 | 3 | 40 |
| 3/8 | 16 | 0.375 | 0.307 | 3 | 24 |
| 7/16 | 14 | 0.438 | 0.360 | 3 | 20 |
| 1/2 | 13 | 0.500 | 0.417 | 3 | 7 |
| 9/16 | 12 | 0.563 | 0.472 | 2 | 59 |
| 5/8 | 11 | 0.625 | 0.527 | 2 | 56 |
| $3 / 4$ | 10 | 0.750 | 0.642 | 2 | 40 |
| 7/8 | 9 | 0.875 | 0.755 | 2 | 31 |
| 1 | 8 | 1.000 | 0.865 | 2 | 29 |

### 9.2 Fine Threads

| Size | Thds. <br> per <br> inch | Major <br> diam. <br> (inches) | Minor <br> diam. <br> (inches) | Lead Angle <br> (deg.) |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $====================================================$ |  |  |  |  |  |
| 0 | 80 | 0.060 | 0.465 | 4 | 23 |
| 1 | 72 | 0.073 | 0.058 | 3 | 57 |
| 2 | 64 | 0.086 | 0.069 | 3 | 45 |
| 3 | 56 | 0.099 | 0.080 | 3 | 43 |
| 4 | 48 | 0.112 | 0.089 | 3 | 51 |
| $================================================$ |  |  |  |  |  |
| 5 | 44 | 0.125 | 0.100 | 3 | 45 |
| 6 | 40 | 0.138 | 0.111 | 3 | 44 |
| 8 | 36 | 0.164 | 0.134 | 3 | 28 |
| 10 | 32 | 0.190 | 0.156 | 3 | 21 |
| 12 | 28 | 0.216 | 0.177 | 3 | 22 |
| $=================================================$ |  |  |  |  |  |
| $1 / 4$ | 28 | 0.250 | 0.211 | 2 | 52 |
| $5 / 16$ | 24 | 0.313 | 0.267 | 2 | 40 |
| $3 / 8$ | 24 | 0.375 | 0.330 | 2 | 11 |
| $7 / 16$ | 20 | 0.438 | 0.338 | 2 | 15 |
| $1 / 2$ | 20 | 0.500 | 0.446 | 1 | 57 |
| $=====================================================$ |  |  |  |  |  |
| $9 / 16$ | 18 | 0.563 | 0.502 | 1 | 55 |
| $5 / 8$ | 18 | 0.625 | 0.565 | 1 | 43 |
| $3 / 4$ | 16 | 0.750 | 0.682 | 1 | 36 |
| $7 / 8$ | 14 | 0.875 | 0.798 | 1 | 34 |
| 1 | 12 | 1.000 | 0.910 | 1 | 36 |

### 9.3 Deflection of Beams

Rectangular Beams, $d=$ vertical direction, $I=l e n g t h, b=$ wide direction, all units in inches, E=Elastic Modulus (lb/in ${ }^{2}$ )
$\mathrm{W}=$ Weight supported (pounds), $\mathrm{h}=$ deflection

| Supported at both ends, | Uniform load | $\mathrm{h}=5 \mathrm{WI}{ }^{3} / 32 \mathrm{Ebd}^{3}$ |
| :--- | :--- | :--- |
| Fixed at both ends, | Uniform load | $\mathrm{h}=\mathrm{WI}^{3} / 32 \mathrm{Ebd}^{3}$ |
| Supported at both ends, | Center load | $\mathrm{h}=\mathrm{WI}^{3} / 4 \mathrm{Ebd}^{3}$ |
| Fixed at both ends, | Center load | $\mathrm{h}=\mathrm{WI}^{3} / 16 \mathrm{Ebd}^{3}$ |

Deflection of Circular flat plates, $R=$ radius(inches), $W=$ total load (pounds), $t=$ thickness (inches)

| Edges supported, | Uniform load | $\mathrm{h}=0.221 \mathrm{WR}^{2} / E t^{3}$ |
| :--- | :--- | :--- |
| Edges fixed, | Uniform load | $\mathrm{h}=0.054 \mathrm{WR}^{2} / E t^{3}$ |
| Edges supported, | Center load | $\mathrm{h}=0.55 \mathrm{WR}^{2} / E t^{3}$ |
| Edges fixed | Center load | $\mathrm{h}=0.22 \mathrm{WR}^{2} / E t^{3}$ |

Metric Note: The formulae above also apply if the lengths are in meters, the weights are in kilograms, and the elastic modulus is in $\mathrm{kg} / \mathrm{m}^{2}$.

Modulus of elasticity

| Material | Elasticity (Millions of $\mathrm{lb} / \mathrm{in}^{2}$ ) |
| :---: | :---: |

$====================================$
Steel, (typical)
Steel, Stainless 28

Aluminum (most types) 10.3
Brass (typical) 15
Titanium 16

| ==================================== |  |
| :--- | :--- |
| Acrylic | 0.40 |
| N |  |

Nylon 0.30

Polyimide
0.37

Alumina 41
Wood
1.4-2.3

### 10.0 REFERENCES

These references are intended to reflect useful references in the field, and they might form a basic library. A short computerized database of references for this formulary is available (for the cost of postage and handling) from North Star Research Corporation.

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